



# Evaluation of Erosion- Sediment Transport Model for a Hillslope Using Laboratory Flume Data

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# INTRODUCTION





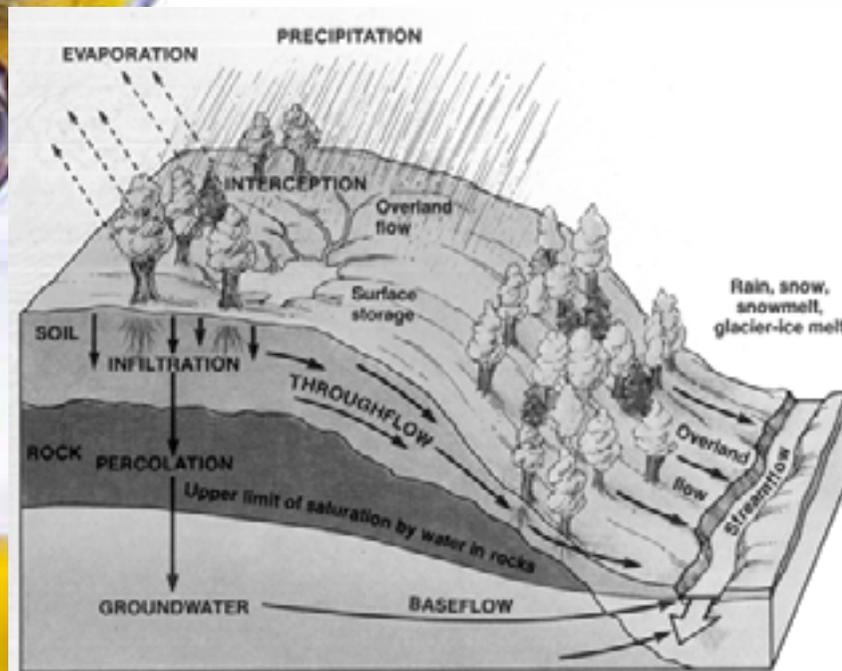
# BACKGROUND

- Climate change  $\Rightarrow$  increase in rainfall



# BACKGROUND

- More overland flow and non-point source pollution (e.g. sediments)  $\Rightarrow$  water quality degradation

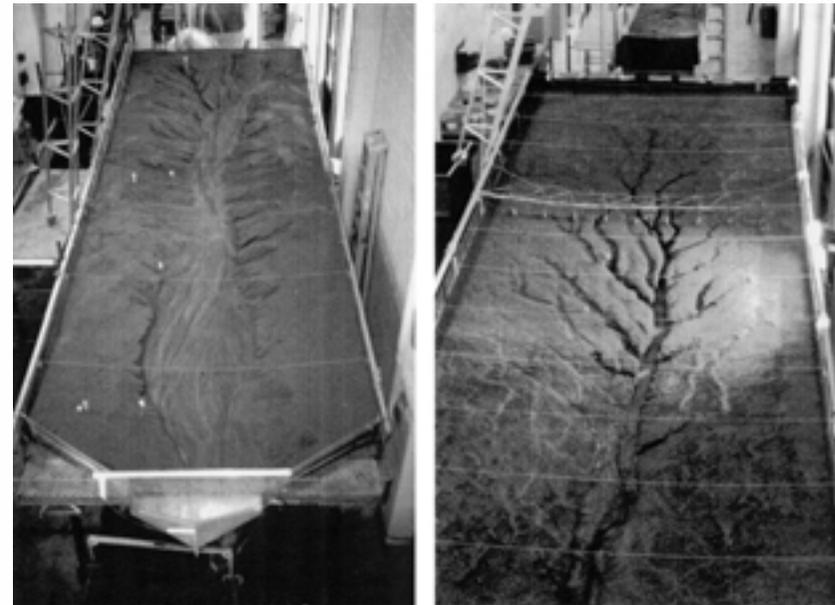


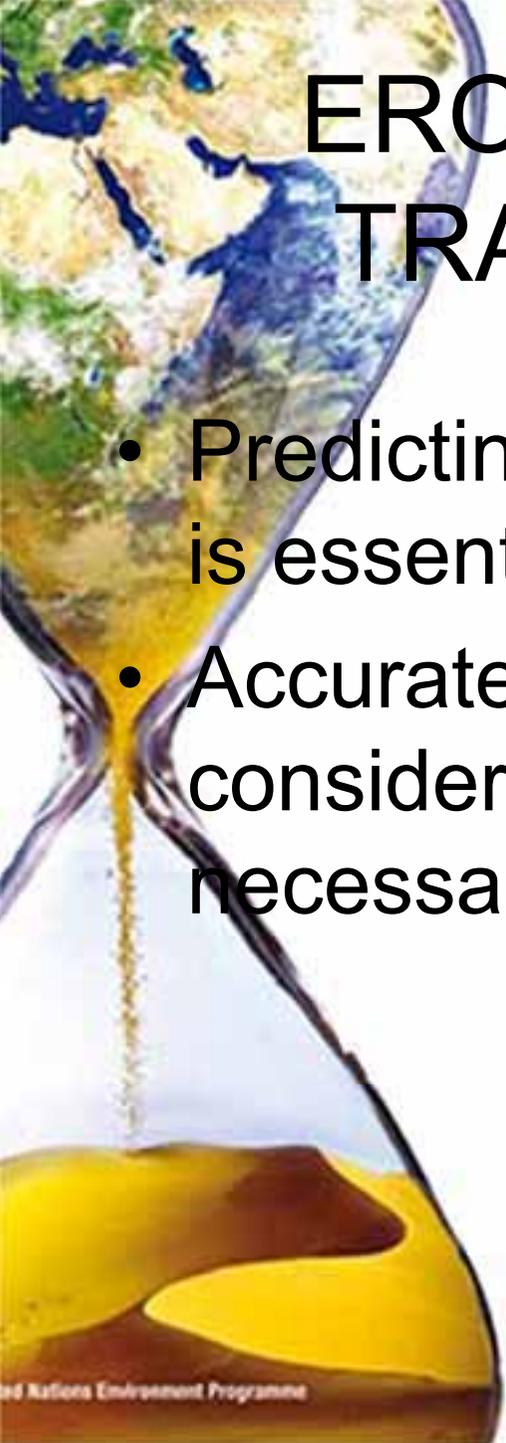
# SOIL EROSION AND LANDSLIDE



# EROSION AND SEDIMENT TRANSPORT ON HILLSLOPES

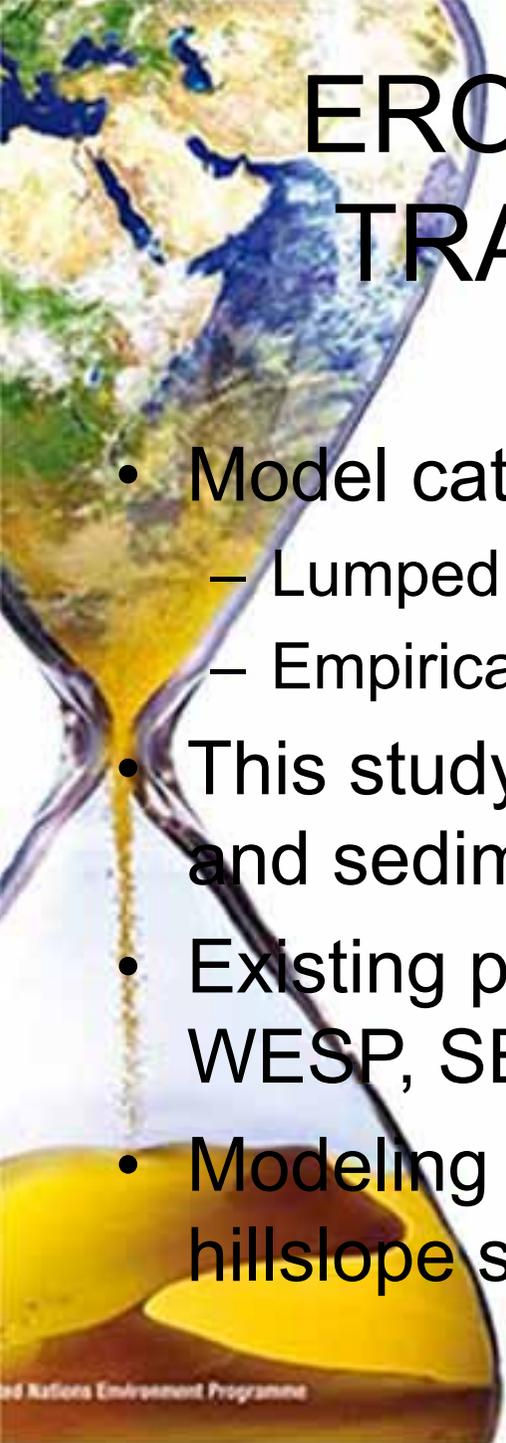
- Rills: small rivulets on hillslopes where runoff is concentrated
- Interrill areas: source areas between the rills
- Rills contain greater flow and sediment discharge than interrill area



An hourglass is shown with the top bulb containing a satellite image of Earth. The sand falling through the neck is a mixture of yellow and brown, representing sediment. The bottom bulb is filled with a similar mixture. The text 'United Nations Environment Programme' is visible at the bottom left of the hourglass.

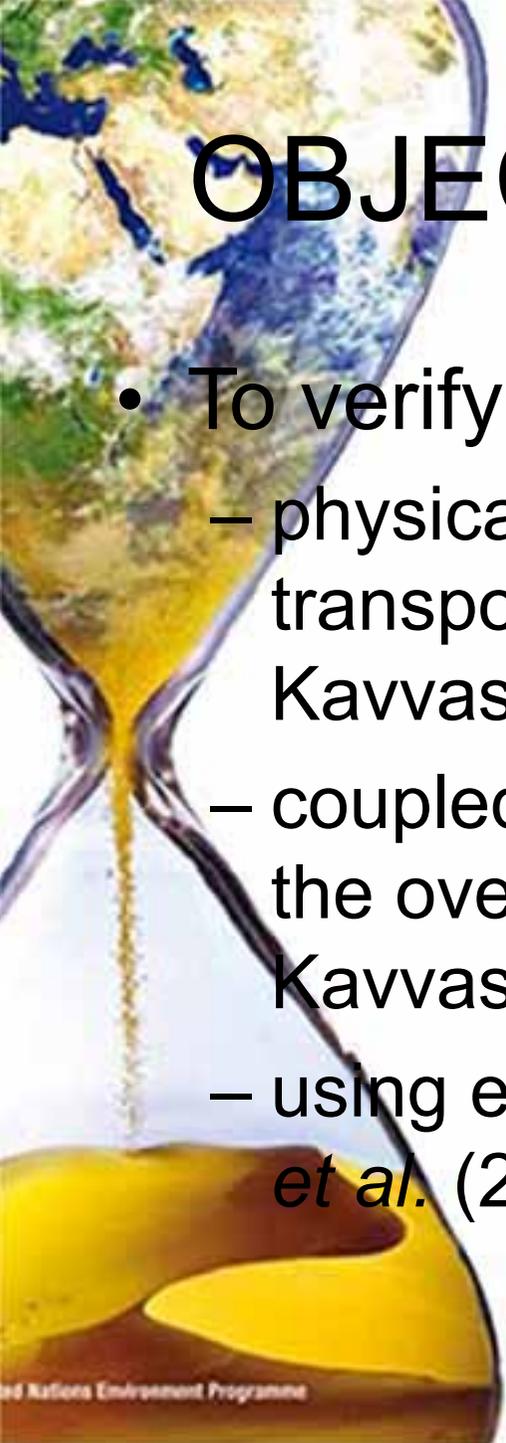
# EROSION AND SEDIMENT TRANSPORT MODELING

- Predicting erosion and sediment transport is essential for water quality management
- Accurate modelling of overland flow considering microtopography of hillslope is necessary for sediment transport modeling

An hourglass is shown with a satellite image of Earth in the upper bulb and yellow sediment in the lower bulb. The title 'EROSION AND SEDIMENT TRANSPORT MODELING' is overlaid on the top half of the image.

# EROSION AND SEDIMENT TRANSPORT MODELING

- Model categories
  - Lumped or distributed
  - Empirical or Physically based
- This study presents a physically based erosion and sediment transport model
- Existing physically based models are KINEROS, WESP, SEM, SHESED, and EUROSEM
- Modeling of erosion and sediment transport at hillslope scale is rarely verified

An hourglass is shown on the left side of the slide. The top bulb contains a satellite image of Earth, showing continents and oceans. The narrow neck of the hourglass is filled with a stream of yellowish-brown sediment falling into the bottom bulb. The bottom bulb is partially filled with a similar sediment. The background is white.

# OBJECTIVE OF THE STUDY

- To verify
  - physically based erosion and sediment transport model developed by Aksoy and Kavvas (2001)
  - coupled to a hillslope hydrological model from the overland flow equations by Yoon and Kavvas (2000)
  - using experimental data acquired from Aksoy *et al.* (2012).

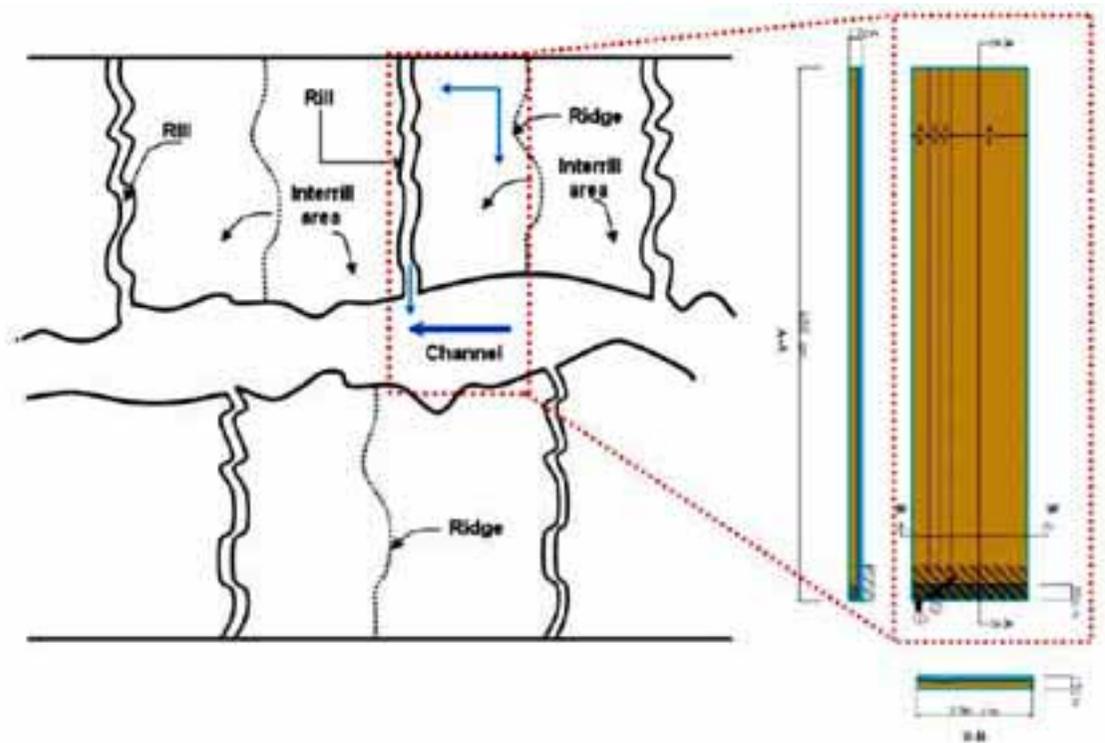
# METHODOLOGY



# EXPERIMENTAL SETUP

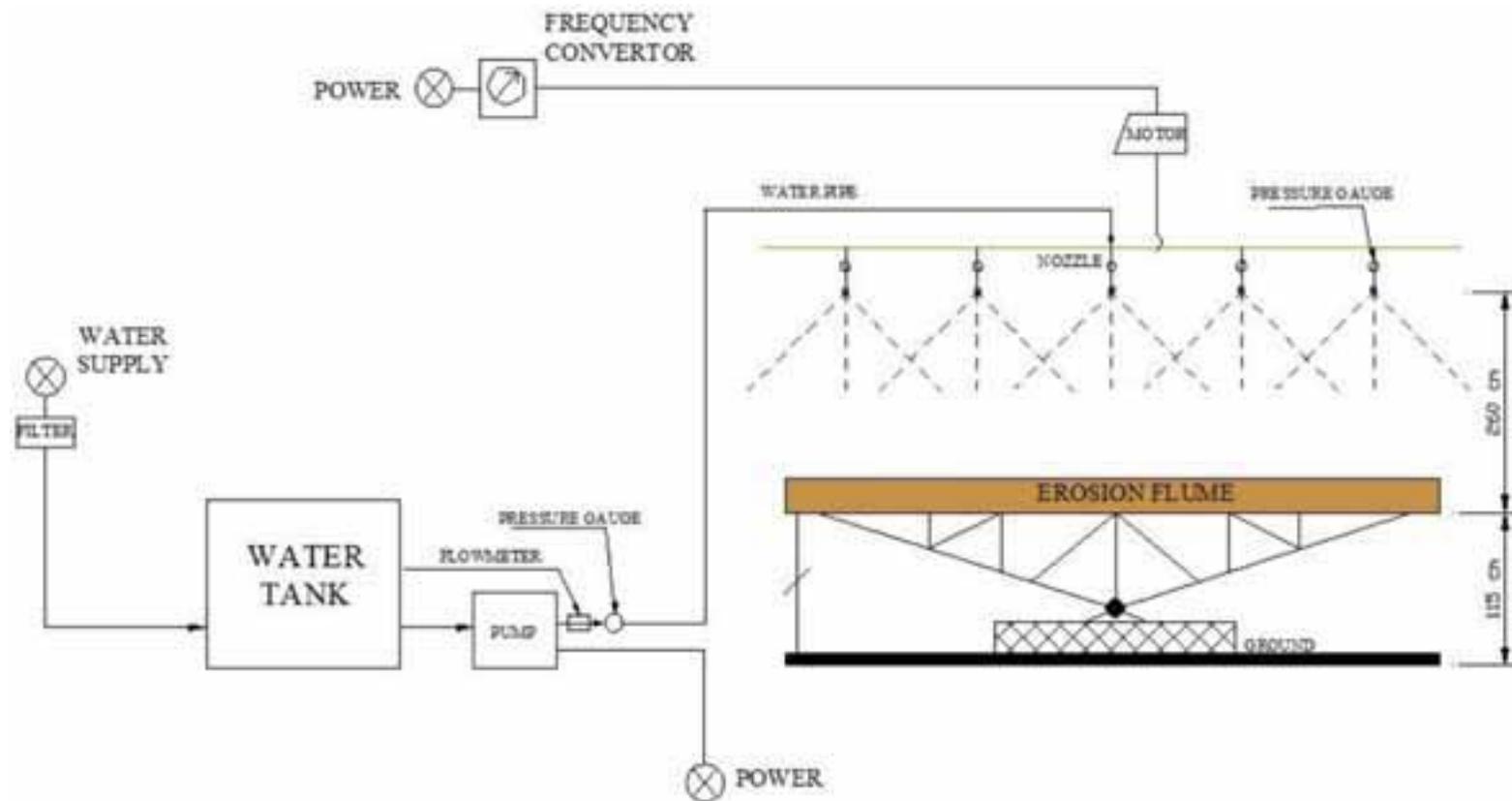
Schematic description of microtopography in a watershed and plan view of the erosion flume (Aksoy *et al.*, 2012)

- 136 cm wide x 650 cm long erosion flume with depth of 17 cm



# EXPERIMENTAL SETUP

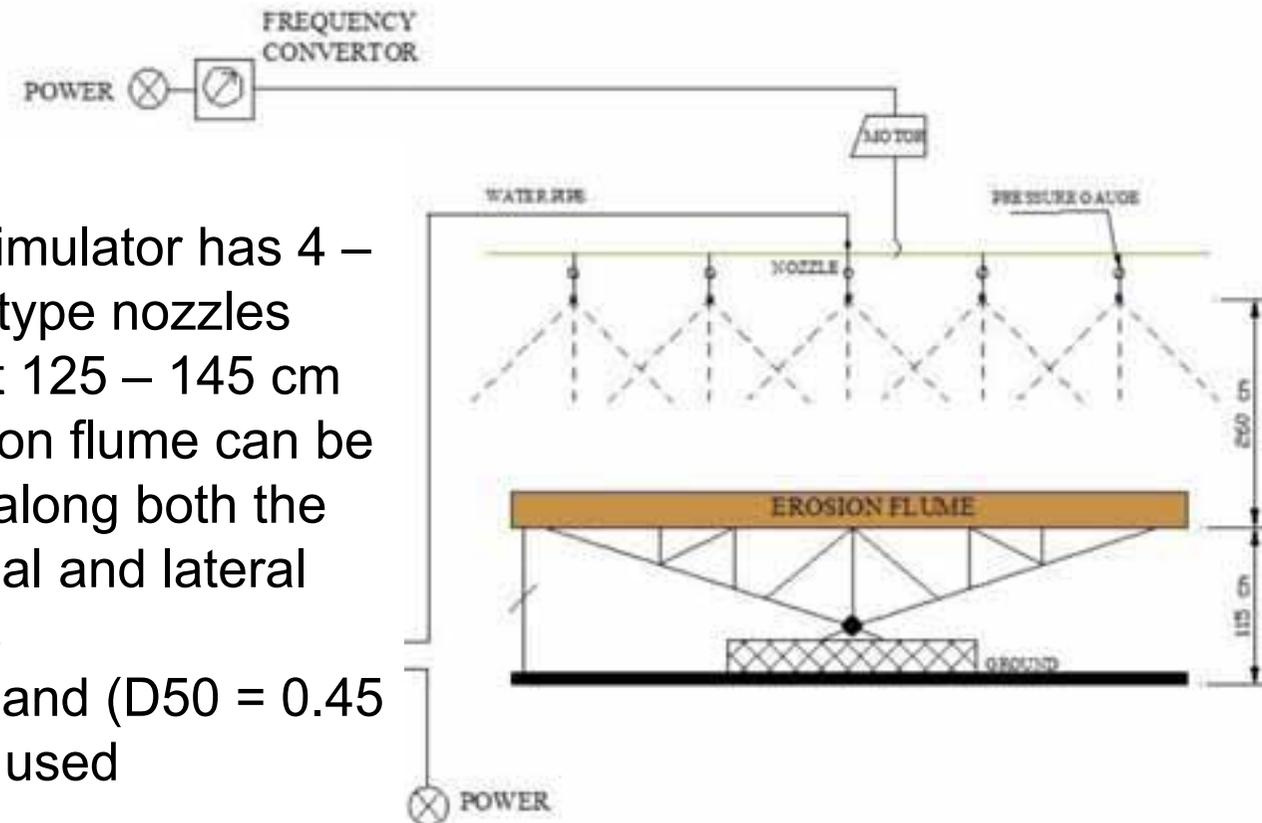
Sketch of rainfall simulator and erosion flume (Aksoy *et al.*, 2012)



# EXPERIMENTAL SETUP

Sketch of rainfall simulator and erosion flume (Aksoy *et al.*, 2012)

- Rainfall simulator has 4 – 5 VeeJet type nozzles spaced at 125 – 145 cm
- The erosion flume can be adjusted along both the longitudinal and lateral directions
- Uniform sand ( $D_{50} = 0.45$  mm) was used



# EXPERIMENTAL SETUP

- Rainfall intensities used were 105 mm/hr and 45 mm/hr and had a duration of 15 minutes for all tests
- The model was calibrated and validated using the experimental results from the setup of the flume having 10 per cent longitudinal and 5 per cent lateral slopes

# MATHEMATICAL MODEL

- Erosion and Sediment Transport Equation for Interrill Area (Aksoy & Kavvas, 2001)

$$K_1 \frac{\partial}{\partial t} [h(x;t)C_s(x;t)] + K_2 \frac{\partial}{\partial x} [[h(x;t)]^{3/2} C_s(x;t)] = \frac{E(x;t)}{\rho_s} - K_3 [[h(x;t)]^{3/2} C_s(x;t)]$$

$$K_1 = \frac{\pi^2}{8}$$

$$K_2 = 0.4577 \left( \frac{\pi}{2} \right)^{5/2} C_x S_{o,x}^{1/2}$$

$$K_3 = \left( \frac{\pi}{2} \right)^{5/2} \frac{1}{l_y} C_y S_{o,y}^{1/2}$$

# MATHEMATICAL MODEL

- The interrill area erosion term is the sum of the rainfall impact erosion and runoff erosion

$$E = \alpha R^\beta + \sigma \left( \eta (\gamma h S_o)^\varepsilon - \rho_s C_s q \right)$$

- $\alpha$  and  $\beta$  are rainfall impact parameters with  $\beta$  set to 1 or 2
- $\sigma$  is the transfer rate coefficient
- $\eta$  and  $\varepsilon$  are dimensionless coefficient and exponent for transport capacity
- $\gamma$  is specific weight of water
- $h$  is flow depth
- $S_o$  is topographical slope
- $\rho_s$  is sediment density
- $C_s$  is volumetric sediment concentration
- $q$  is discharge

# MATHEMATICAL MODEL

- Erosion and Sediment Transport Equation for Rill (Aksoy & Kavvas, 2001)

$$\frac{\partial}{\partial t} [A_R(h_R)C_{s,R}] + \frac{\partial}{\partial x} [Q_R(h_R)C_{s,R}] = \frac{1}{\rho_s} (E_R + q_{s,IR})$$

$$A_R(h_R) = b_R h_R$$

$$Q_R(h_R) = C_R \sqrt{S_R} \left[ \frac{(b_R h_R)^3}{b_R + 2h_R} \right]^{1/2}$$

# MATHEMATICAL MODEL

- The rill erosion term is defined as

$$E_R(x,t) = \sigma \rho_s b \left[ gS \frac{bh(x,t)}{b + 2h(x,t)} \right]^{1/2} 0.635 D [\delta(x,t) - 2.5 \ln(1 + 0.4\delta(x,t))] \\ - \sigma \rho_s 0.4577 \left( \frac{\pi}{2} \right)^5 C_y \sqrt{S_{oy}} C_s(t) [h(t)]^{3/2}$$

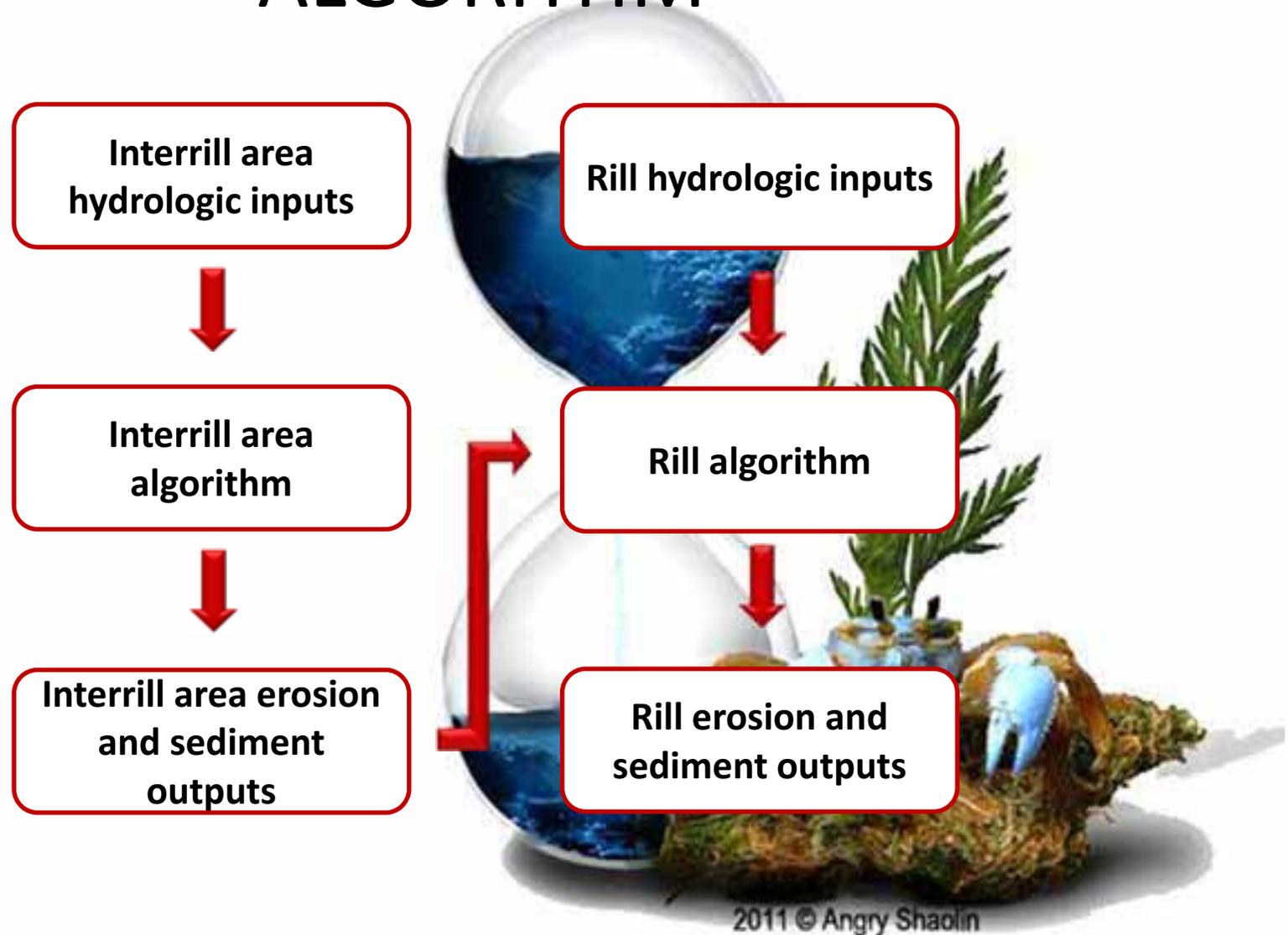
where

$$\delta(x,t) = \frac{\gamma}{\tau_c (\gamma - \gamma_s)} \frac{S}{D} \frac{bh(x,t)}{b + 2h(x,t)} - 1$$

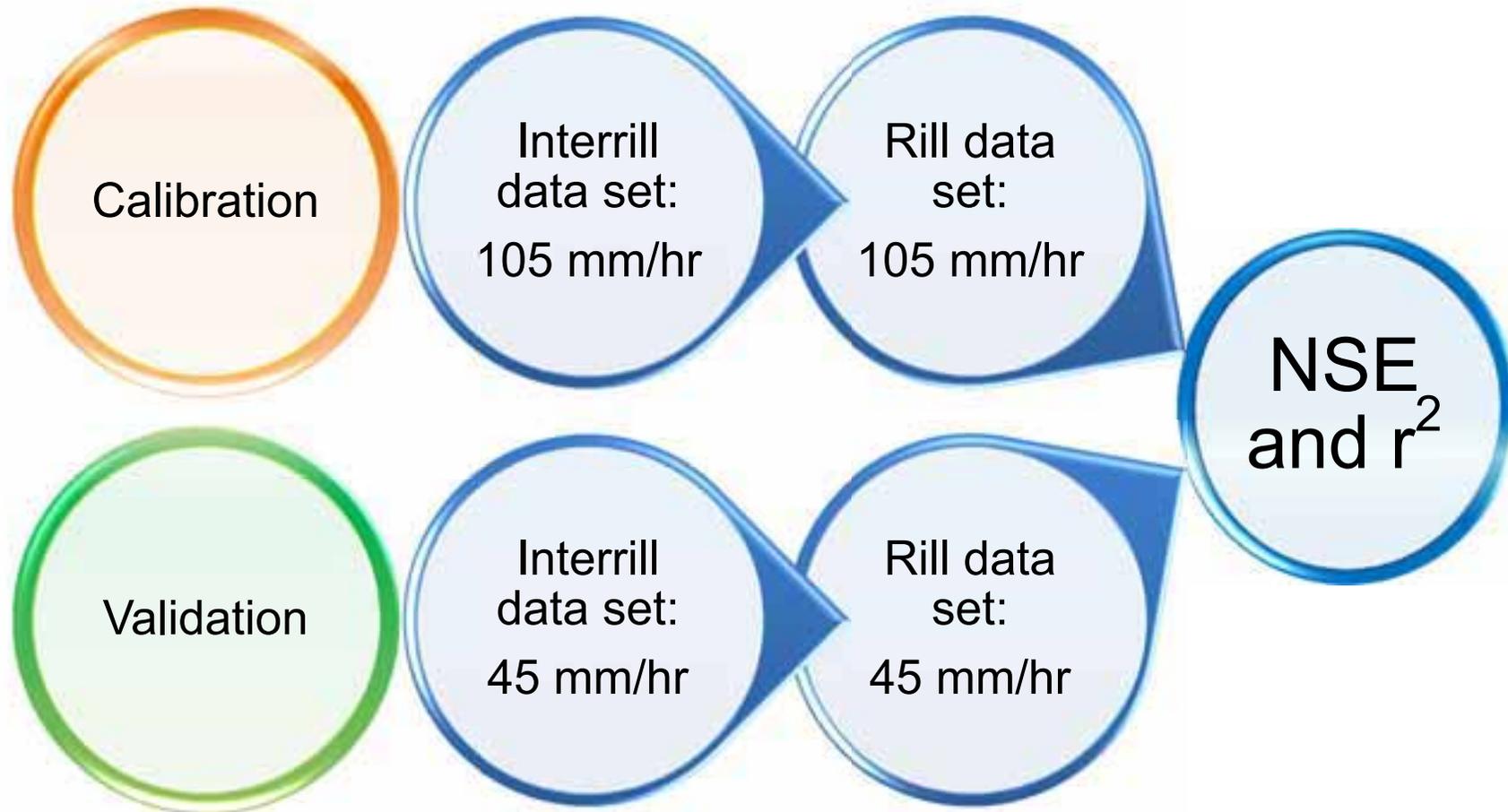
# MATHEMATICAL MODEL

- $\sigma$  is the rill transfer rate coefficient
- $\rho_s$  is sediment density
- $b$  is rill width
- $S$  is slope along the rill
- $D$  is sediment diameter
- $C_s$  is volumetric sediment concentration
- $C_y$  is Chezy coefficient
- $\tau_c$  is critical shear stress

# STRUCTURE OF DEVELOPED ALGORITHM



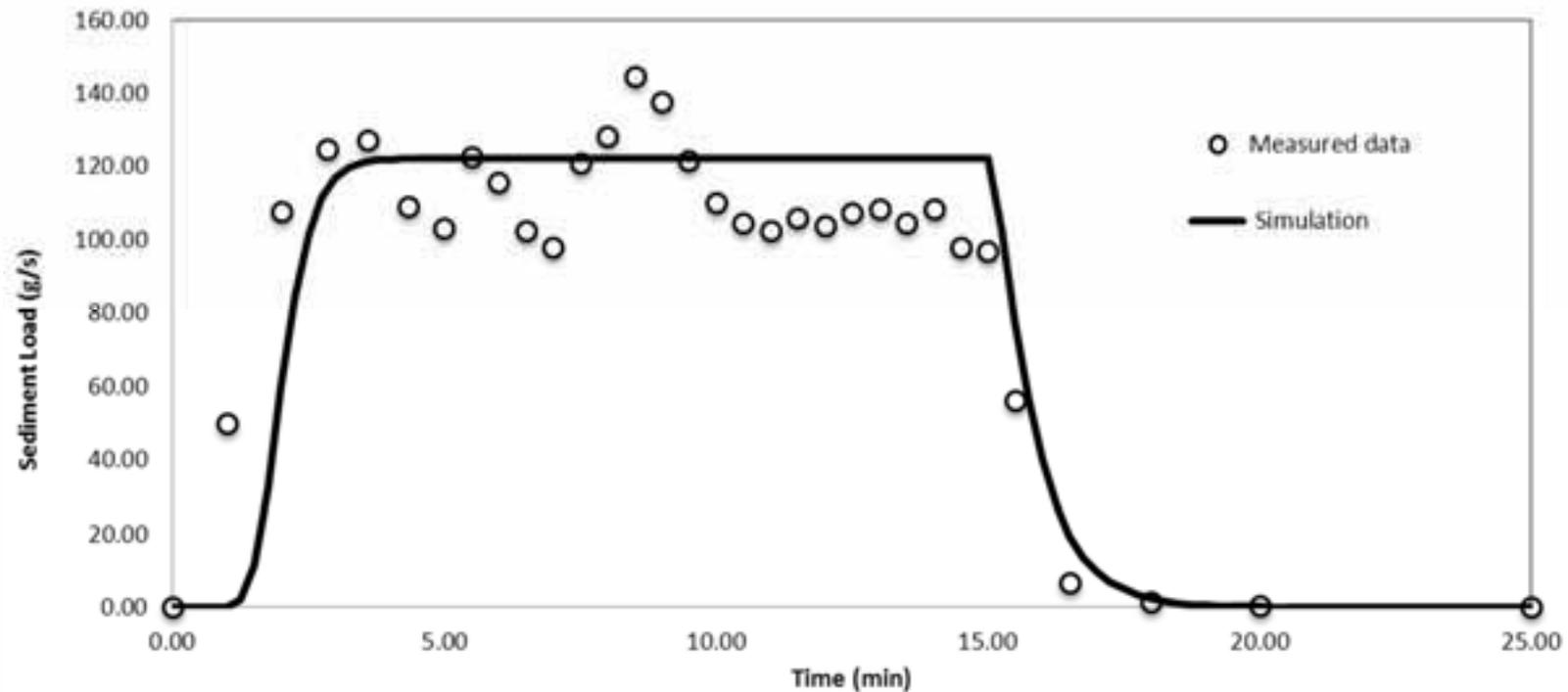
# CALIBRATION & VALIDATION



# RESULTS

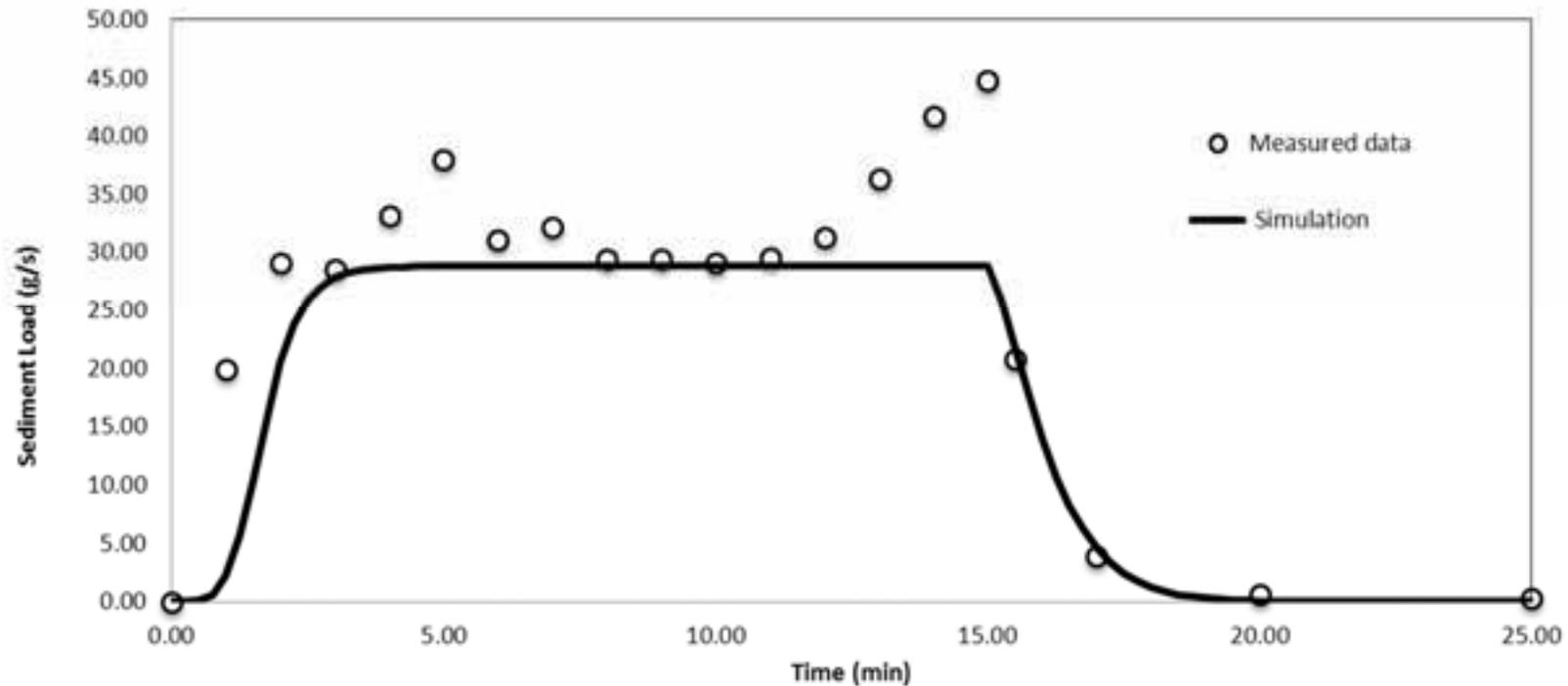


# CALIBRATION (Interrill Area-Rill)



Intensity (mm/hr)	Interrill					Rill		$r^2$	NSE
	$\alpha$ (-)	$\beta$ (-)	$\sigma$ ( $m^{-1}$ )	$\eta$ (-)	$\epsilon$ (-)	$\sigma_r$ ( $m^{-1}$ )	$\tau_c$ (-)		
105	1.00	1.00	1.00	0.035	1.00	0.053	0.060	0.84	0.80

# VALIDATION (Interrill Area-Rill)



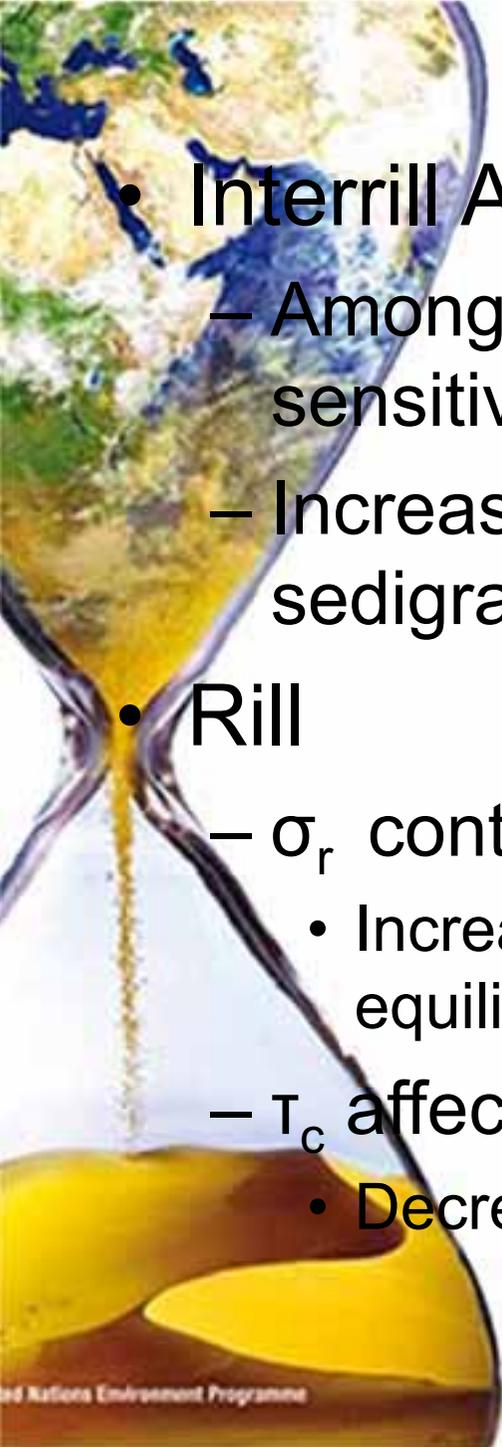
Intensity (mm/hr)	Interrill					Rill		$r^2$	NSE
	$\alpha$ (-)	$\beta$ (-)	$\sigma$ (m <sup>-1</sup> )	$\eta$ (-)	$\epsilon$ (-)	$\sigma_r$ (m <sup>-1</sup> )	$\tau_c$ (-)		
45	1.00	1.00	1.00	0.035	1.00	0.053	0.060	0.83	0.72

# SUMMARY OF RESULTS

Intensity (mm/hr)	Interrill			Rill		$r^2$	NSE
	$\sigma$ (m <sup>-1</sup> )	$\eta$ (-)	$\varepsilon$ (-)	$\sigma_r$ (m <sup>-1</sup> )	$\tau_c$ (-)		
105	1.00	0.035	1.00	0.053	0.060	0.84	0.80
45	1.00	0.035	1.00	0.053	0.060	0.83	0.72

An hourglass is shown on the left side of the slide. The top bulb contains a small globe of the Earth with blue oceans and green landmasses. The bottom bulb contains a mixture of yellow and brown liquids, representing water. A thin stream of yellow liquid is falling from the narrow neck of the hourglass. The background is white.

# **DISCUSSION AND CONCLUSION**

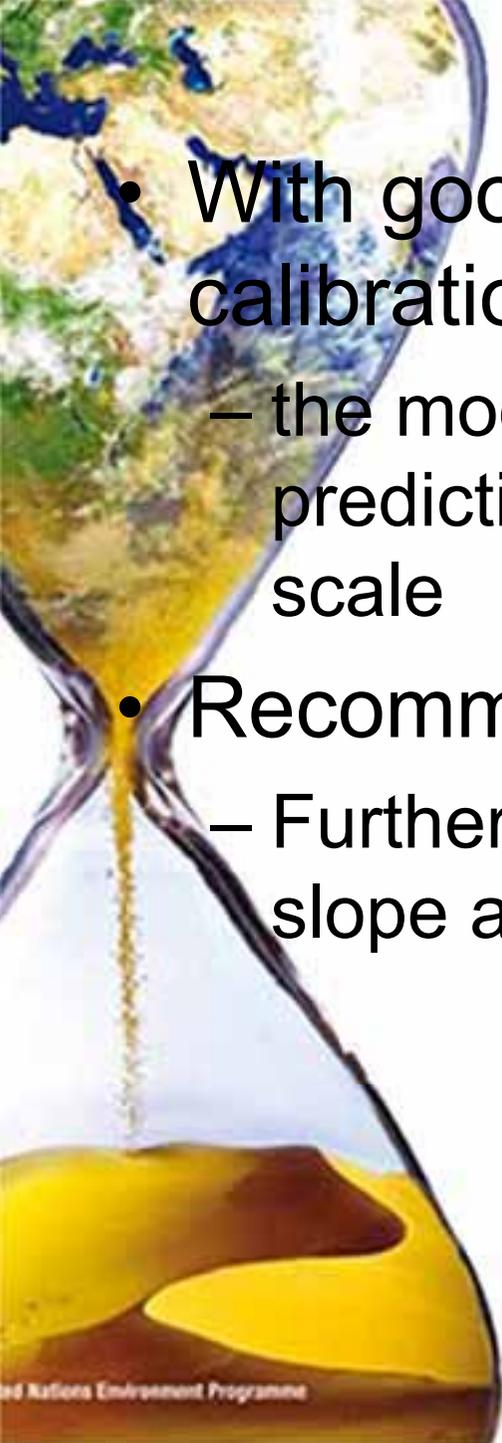


- Interrill Area

- Among the 5 calibration parameters, the most sensitive parameter was  $\eta$
- Increasing  $\eta$  also increased the peak of the sedigraph

- Rill

- $\sigma_r$  controlled the magnitude
  - Increasing its value makes sedigraph reach equilibrium faster
- $\tau_c$  affected the peak of the sedigraph
  - Decreasing its value increased the peak

- 
- An hourglass is shown with a globe of the Earth in the upper bulb and sediment in the lower bulb. The globe is tilted, and the sediment is being poured from it. The sediment is a mix of yellow and brown colors. The hourglass is positioned on the left side of the slide, and the text is on the right.
- With good statistical performance for both calibration and validation
    - the model is thought to be a promising tool for predicting sediment discharge at hillslope scale
  - Recommendation for future studies
    - Further validation of the model with more slope and rainfall combinations



# ACKNOWLEDGEMENT

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**Thank you!**



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